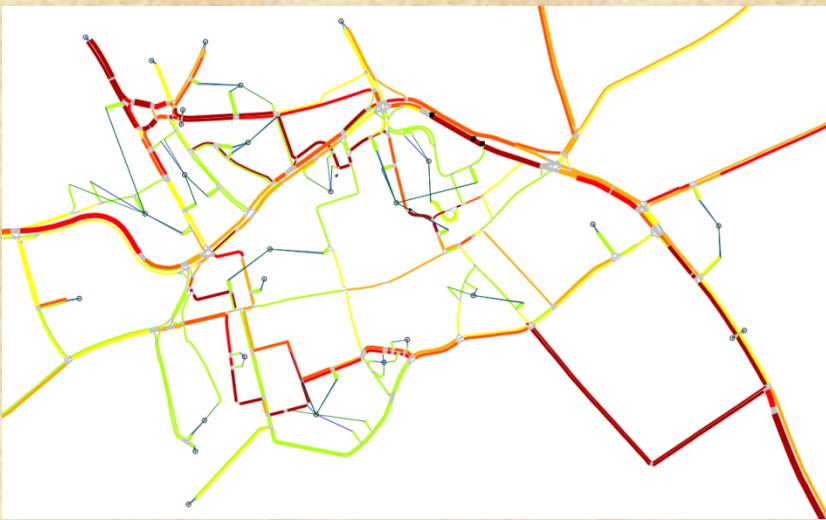


BI-LEVEL OPTIMIZATION MODELS FOR ADJUSTMENT OF TIME-SLICED OD MATRICES



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Academic Director of CARNET (Cooperative Automotive Research Network)

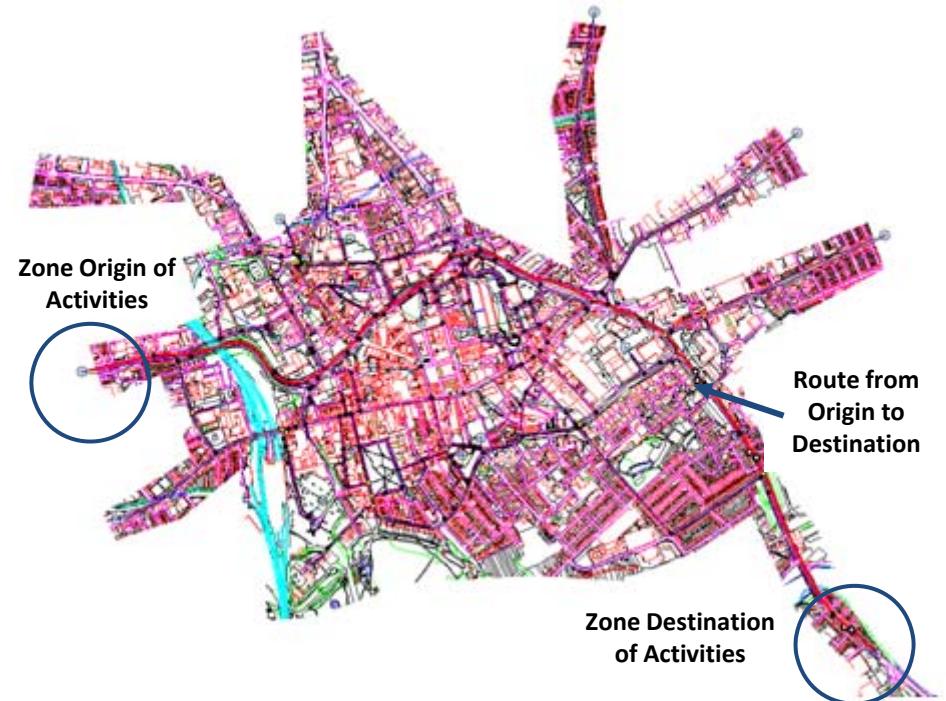
THE SYSTEMS MODELING APPROACH

- Applying the OR methodology to transportation systems
- Understanding the system and how the system works:
 - Components and interactions
 - Formulate modeling hypothesis capturing them
 - Translate modeling hypothesis in terms of a formal representation of the system: the model (or theory)
- “Toda a teoria deve ser feita para poder ser posta em prática, e toda prática deve obedecer a uma teoria.... teoria e a prática complementam-se. Foram feitas a uma para a outra”

(Fernando Pessoa, Revista da Contabilidade, No. 1, p. 5, Janeiro de 1926).

UNDERSTANDING THE MOBILITY OF PERSONS AND FREIGHT

- Mobility is the movement of people and goods efficiently and safely and may be regarded as the ability to travel (**When and where the traveler needs, in the most efficient way**)
- Mobility is a derived demand and, as such, means for enabling people and freight to **access** other people and places to realize activities
- Mobility is thus a mean to the end of **accessibility**
- Mobility must ensure the realization of accessibility: **citizens and freight must reach destinations to satisfy needs and have access to places where activities happen**
- **Mobility patterns** are a consequence of the space and time distribution of these activities
- ⇒ Points (zones) where activities are either “**generated**” or “**attracted**” (TAZ transport analysis zones)
- ⇒ **Paths** connecting (giving access) origins and destinations



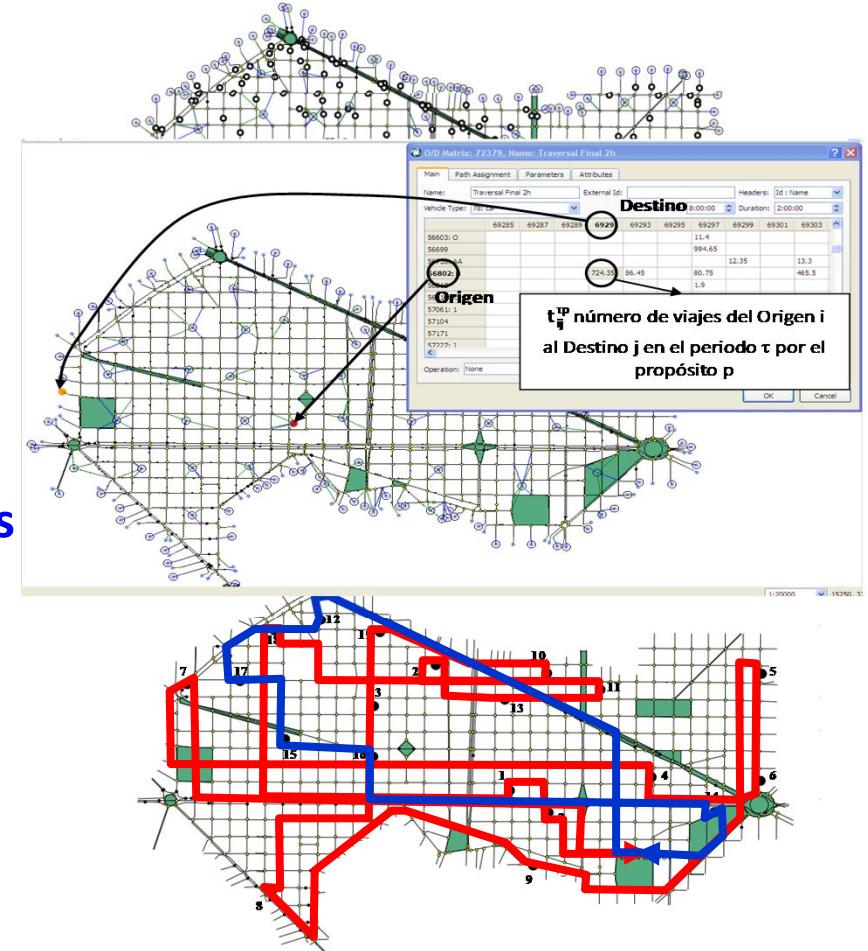
CARACTERIZING MOBILITY

In terms of mobility patterns:

- Trip matrices (origin-destination)
- Number of trips from an origin to a destination for a given purpose (home to work, leisure, shopping, others) in a given time period.

In terms of itineraries, alternative routes between origins and destinations:

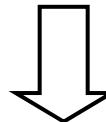
- Computation of time dependent paths
- Modeling the route choice selection processes



FORMULATING MODELING HYPOTHESIS USER EQUILIBRIUM (WARDROP)

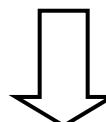
BEHAVIORAL ASSUMPTION

Each user chooses the route that he perceives the best in terms of travel time



CONSEQUENCE

If there exists a shorter route than the one a user is using, he will choose it



EQUILIBRIUM

No user can improve (unilaterally) his travel time

MODELING USER EQUILIBRIUM

Flows on a network are in equilibrium that satisfies Wardrop's user principle when for (r, s) OD - pair, path flows f_{rsp}^* and minimum path costs θ_{rs}^* :

$$\begin{aligned} & (\tau_{rsp} - \theta_{rs}^*) f_{rsp}^* = 0, \forall p \in P_{rs}, \forall (r, s) \in \mathfrak{J} \\ & (\tau_{rsp} - \theta_{rs}^*) \geq 0 \quad \forall p \in P_{rs}, \forall (r, s) \in \mathfrak{J} \\ & \sum_{p \in P_{rs}} f_{rsp} - d_{rs} = 0 \quad \forall (r, s) \in \mathfrak{J} \\ & f_{rsp}^* \geq 0, \theta_{rs}^* \geq 0 \end{aligned}$$

$$f(v^*)(v - v^*) \geq 0$$

Smith's Variational Inequality (1979)

$$\left\{ \begin{array}{l} \text{Left side: } \\ \left(\tau_{rsp} - \theta_{rs}^* \right) f_{rsp}^* = 0, \forall p \in P_{rs}, \forall (r, s) \in \mathfrak{J} \\ \left(\tau_{rsp} - \theta_{rs}^* \right) \geq 0 \quad \forall p \in P_{rs}, \forall (r, s) \in \mathfrak{J} \\ \sum_{p \in P_{rs}} f_{rsp} - d_{rs} = 0 \quad \forall (r, s) \in \mathfrak{J} \\ f_{rsp}^* \geq 0, \theta_{rs}^* \geq 0 \end{array} \right\} \Leftrightarrow \left\{ \begin{array}{l} \text{Right side: } \\ f(v^*)(v - v^*) \geq 0 \\ v \in \Theta = \left\{ \begin{array}{l} v : v_a = \sum_{p \in P_{rs}} \sum_{(r, s) \in \mathfrak{J}} \delta_{ap} f_{prs}, \\ \sum_{p \in P_{rs}} f_{rsp} - d_{rs} = 0 \quad \forall (r, s) \in \mathfrak{J} \end{array} \right\} \end{array} \right\}$$

M. Florian and D. Hearn, Network Equilibrium Models and Algorithms, Chapter 6 in:
 M.O. Ball et al., Eds., Handbooks in OR and MS, Vol.8, Elsevier Science B.V. (1995).

MATHEMATICAL MODEL (Separable case)

$$\text{Min} \sum_{a \in A} \int_0^{v_a} s_a(x) dx + \sum_{c \in C} \sum_{a \in A} v_a^c \theta^c t_a^c$$

s.t.

$$\sum_{k \in K_i} h_k = g_i \quad \forall i \in I, \quad (I = \{\text{set of O/D pairs}\})$$

$$h_k \geq 0, \text{ (flow on path } k), \quad v_a = \sum_{i \in I} \sum_{k \in K_i} h_k \delta_{ak}$$

g_i , demand for the i -th O/D pair

$K_i = \{\text{set of paths connecting the } i\text{-th O/D pair}\}$

- Mathematical model: non-linear network flow model
- Algorithms: Frank and Wolfe, RSD, etc.
- Model size: usually large networks (urban or metropolitan road networks)
- Model uses: strategic transport planning, medium to long term effects

MICROSCOPIC SIMULATION MODEL BUILDING

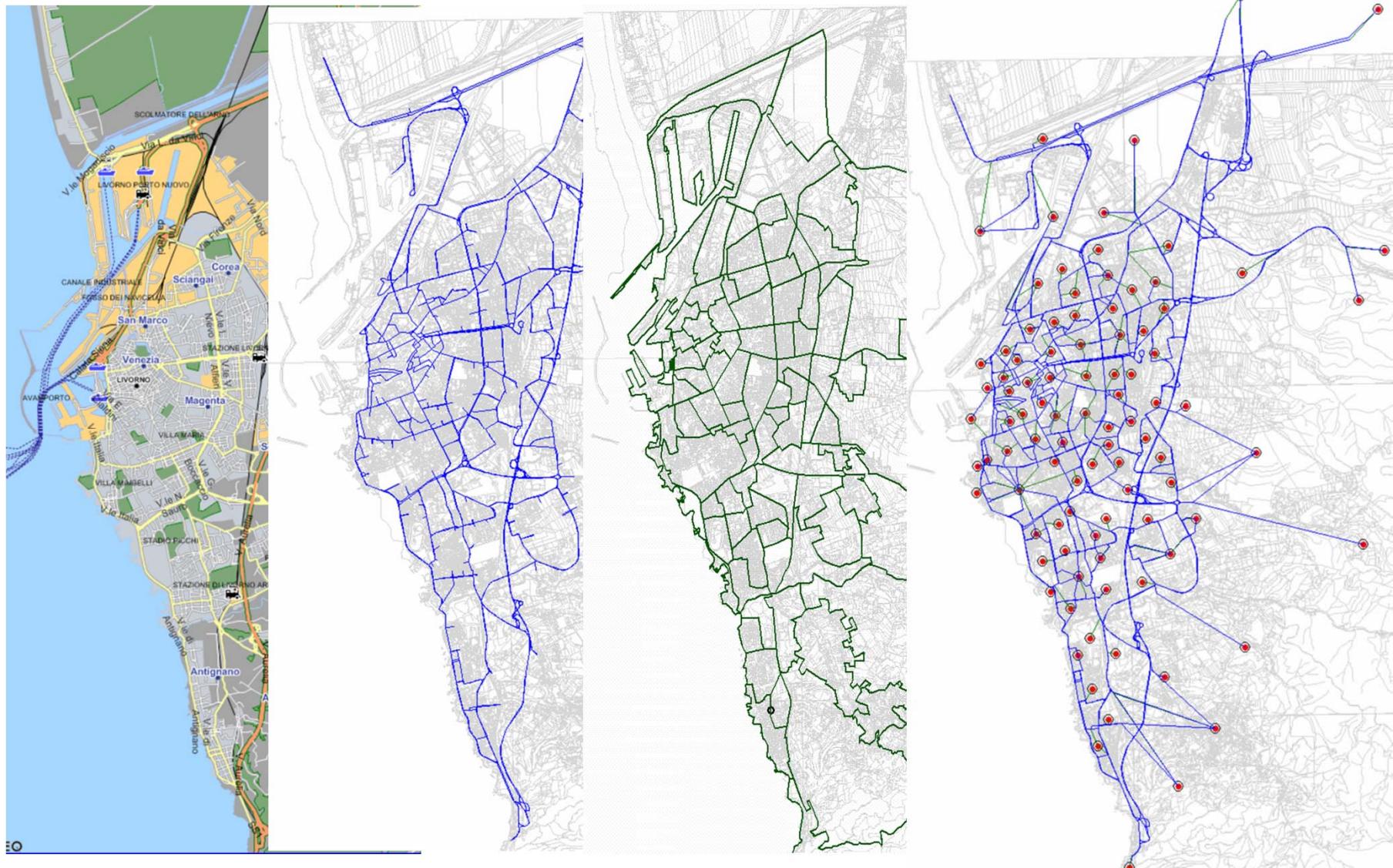
Network → Import + Edit → TAZ →



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UNIVERSITAT POLITÈCNICA DE CATALUNYA

Import OD



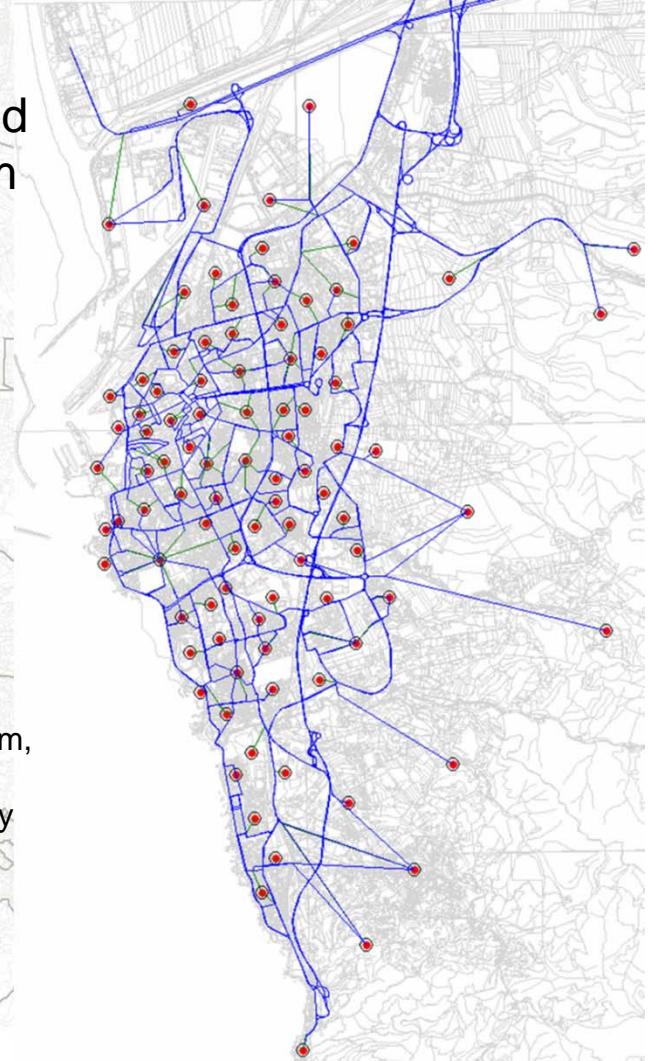
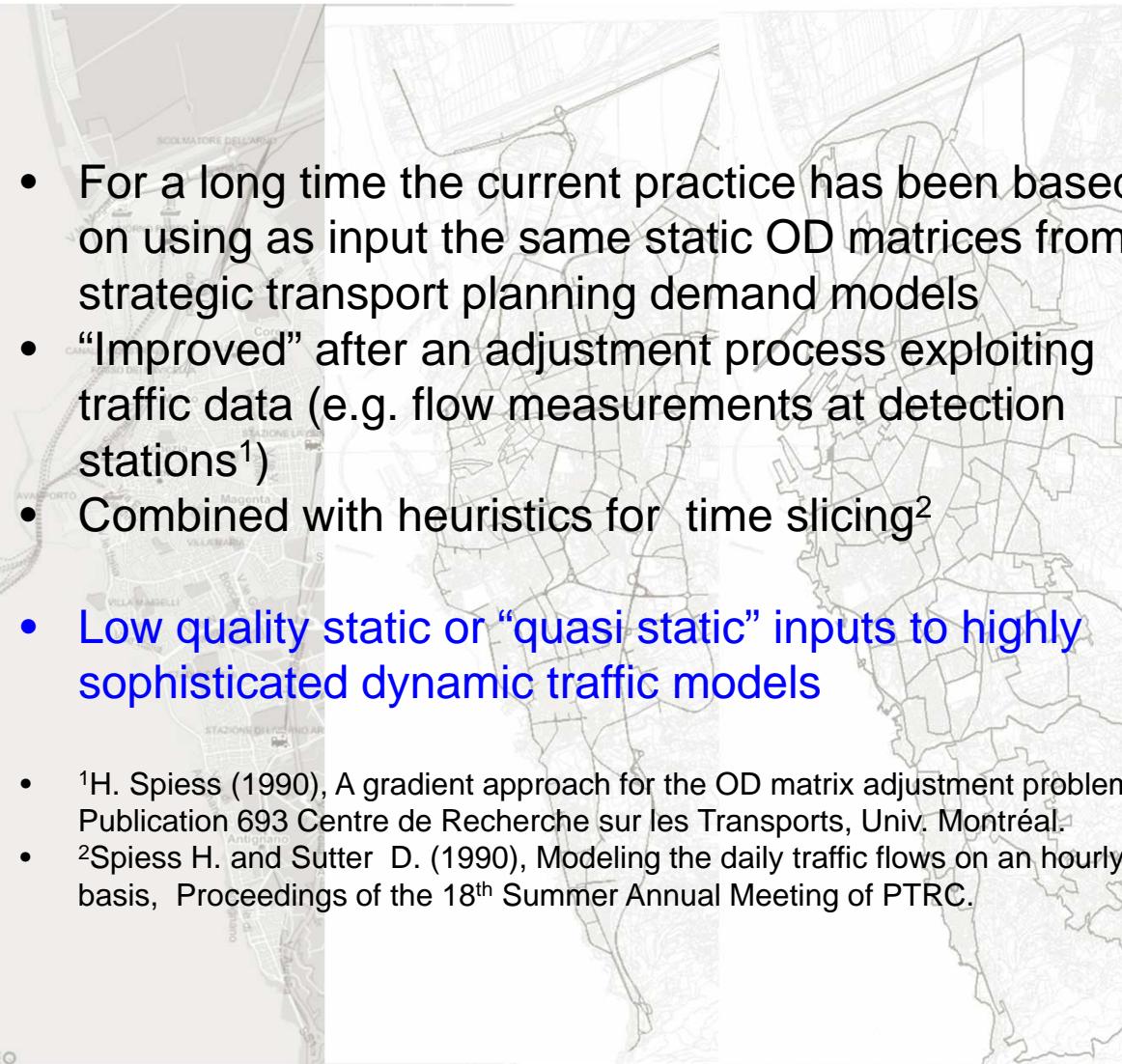
J. Barceló/Bi-level optimization models for adjustment of time-sliced OD matrices

MICROSCOPIC SIMULATION MODEL BUILDING

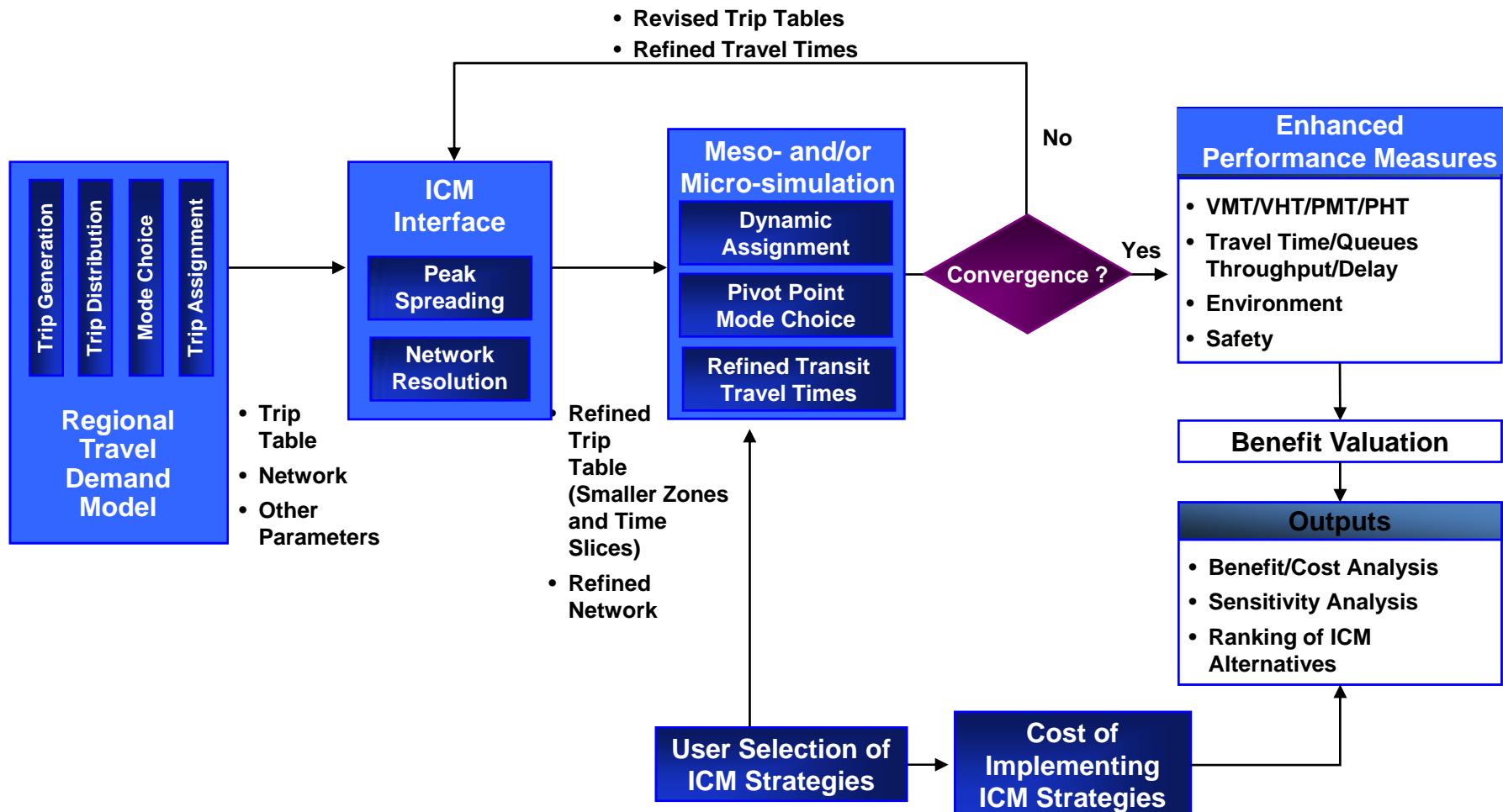
Network → Import + Edit → TAZ →



Import OD



INTEGRATED CORRIDOR MANAGEMENT (ICM) ANALYSIS, SIMULATION MODELING (AMS) APPROACH



Source: V. Alexiadis and D. Sallman, Cambridge Systematics; A. Armstrong, SAIC, (2012), Traffic Analysis Toolbox Volume XIII: Integrated Corridor Management Analysis, Modeling, and Simulation Guide, Report No. FHWA-JPO-12-074

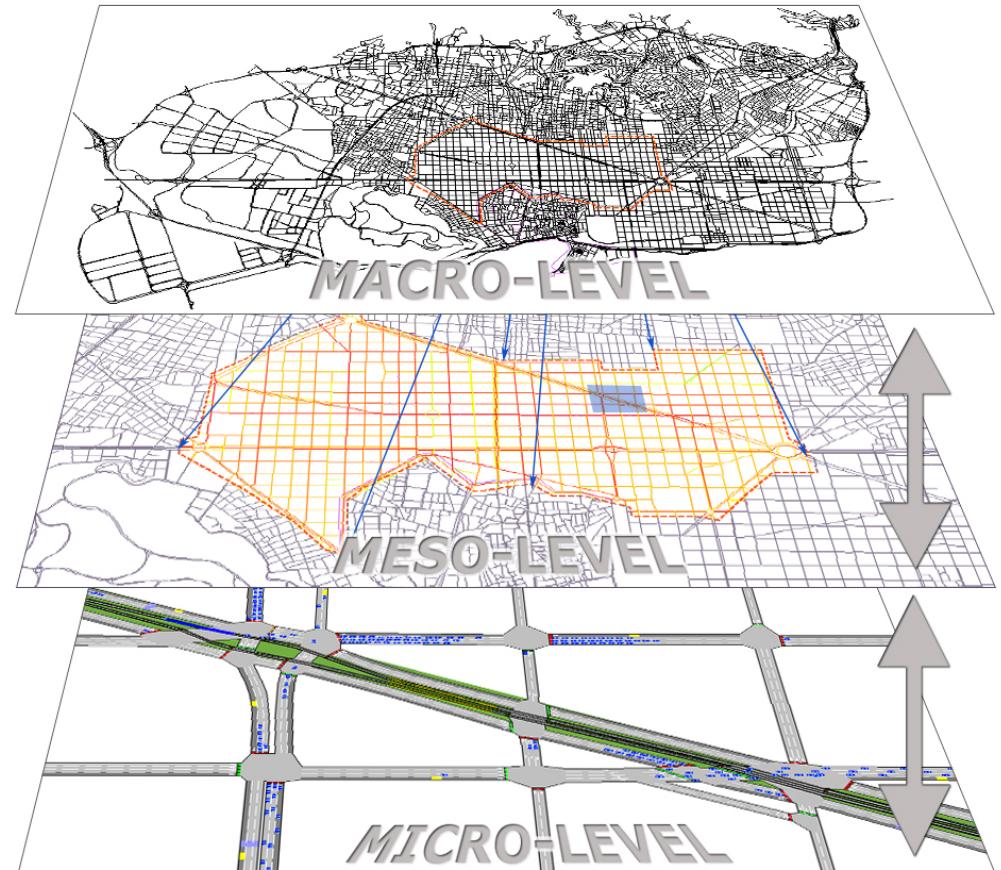
MODELS USED IN INTEGRATED TRANSPORTATION ANALYSIS



	Travel Demand Models	Mesoscopic Simulation Models	Microscopic Simulation Models
Geographic Coverage	Regional Network / Metropolitan Area 	Regional Network / Metropolitan Area 	Small to medium size subarea networks
Demand	Static O-Ds	Dynamic OD-s	Dynamic OD-s
Traffic Control	No signal settings	Detailed signal setting & phasing schemes	Detailed signal setting & phasing schemes
Analysis	User equilibrium assignment link costs defined in terms of volume-delay functions	Dynamic user equilibrium based on simulation based network loading	Behavioral modeling based on car-following, lane changing and route choice of individual vehicles
Advantages	Available from local MPO; can analyze mode shift. Low calibration effort	Can analyze regional dynamic diversion. Brings the dynamic dimension into planning analysis. Moderate calibration effort	Suitable for detailed dynamic analysis of operational strategies such as ramp metering, traffic signal coordination and ITS
Limitations	Not sensitive to operational strategies; not capable of analyzing regional dynamic diversion	Not yet capable of analyzing mode shift	Data availability for proper calibration

FROM MACRO TO MESO AND MICRO

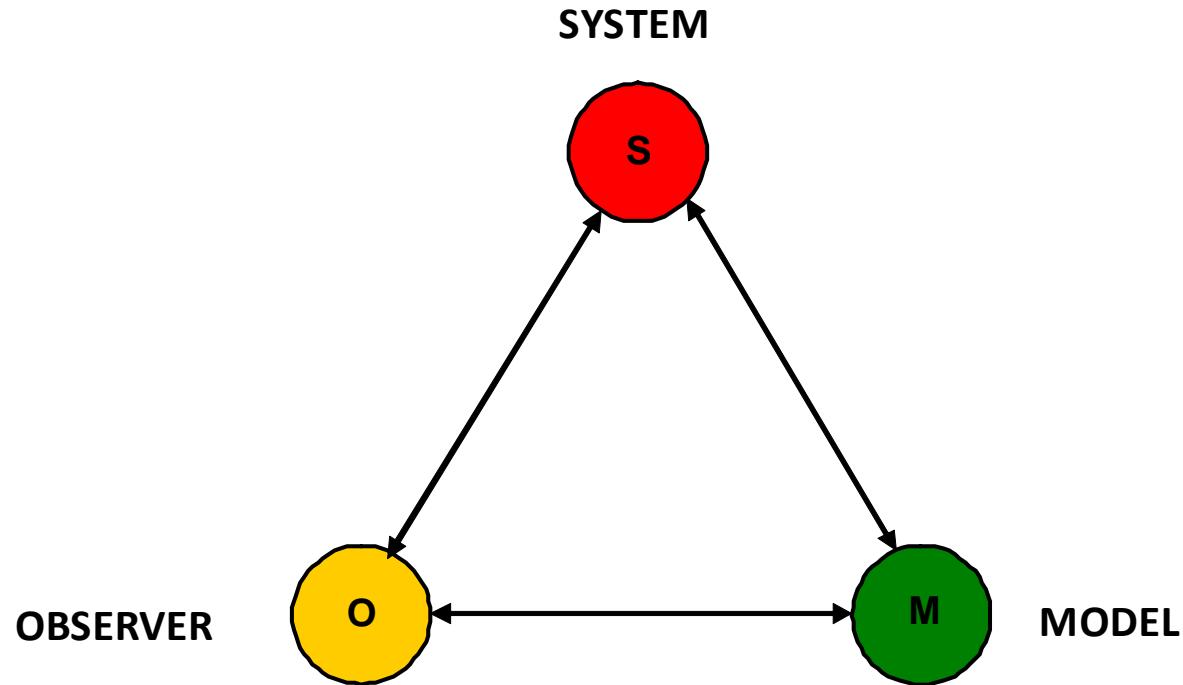
- The question is not whether one approach is better or more appropriate than other
- Or if there is a unique approach that can replace satisfactorily all others
- But which is the most appropriate use of each approach and how can them work together in a fully integrated common framework



J. Barceló et al. (2005), Methodological notes on combining macro, meso and micro models for transportation analysis, Workshop on Traffic Modeling(*Simulation Models: From the Labs to the Trenches*), Sedona, 2005.

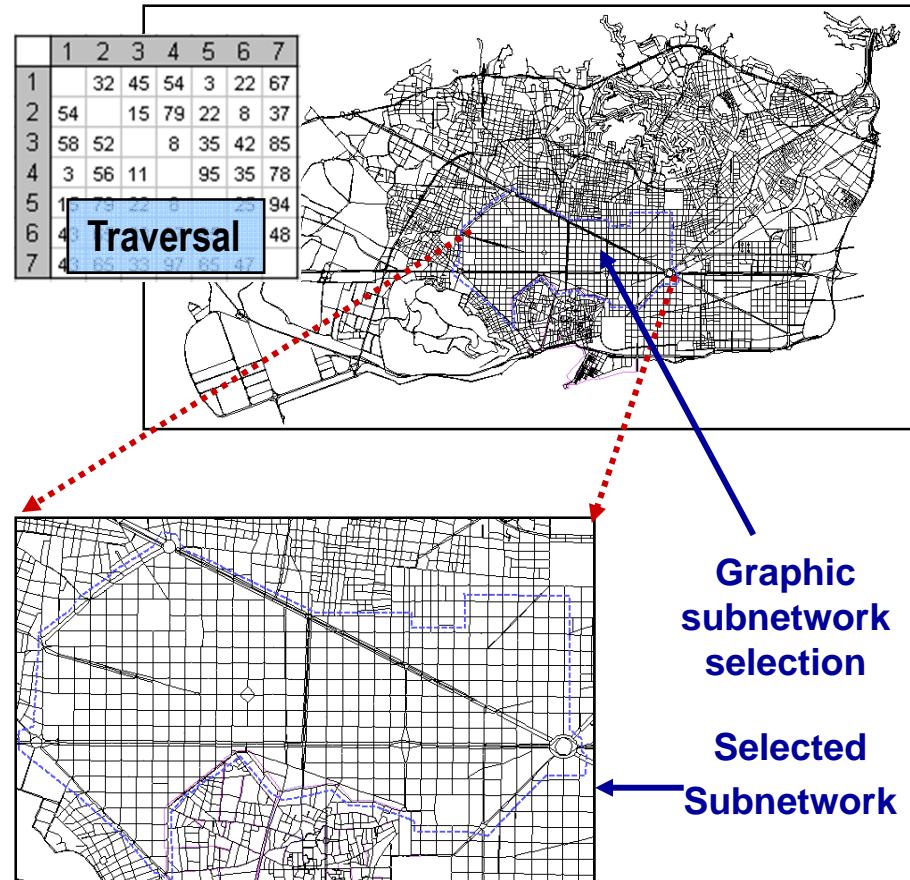
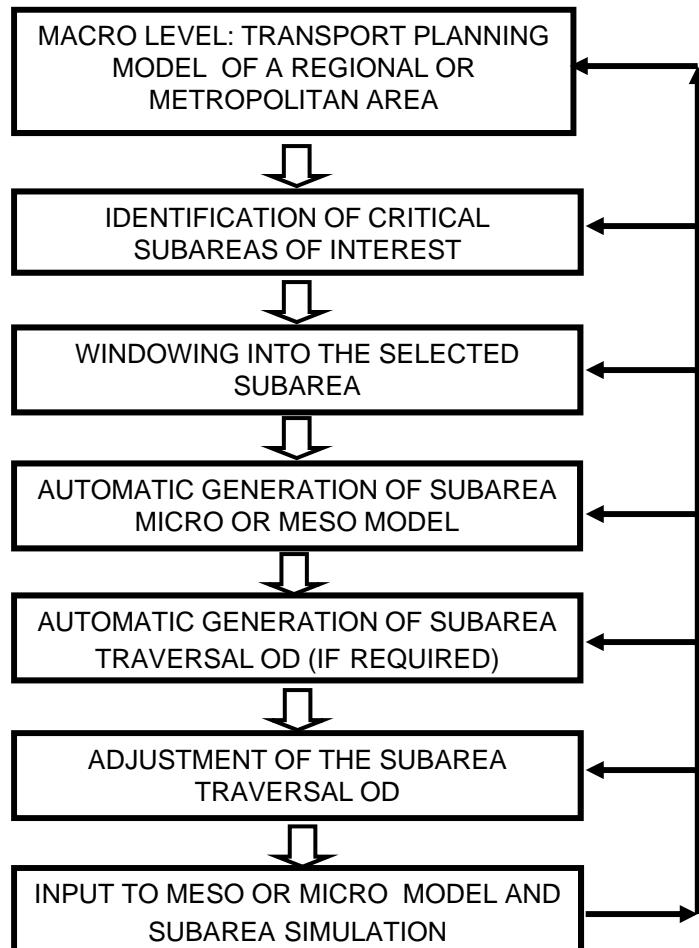
J. Barceló, J. Casas, D. García and J. Perarnau , A hybrid simulation framework for advanced transportation analysis, ISTS06 (International Symposium on Traffic Simulation 2006), Lausanne, 2006

SYSTEMS, OBSERVERS, MODELS



- An **object M** is a *model* of a **system S** if it can provide valid answers to the questions of an **observer O** on the system S (Minsky)

THE METHODOLOGICAL PROCESS COMBINING MACRO↔MESO↔MICRO



DYNAMIC TRAFFIC ASSIGNMENT (DTA)

- Advanced Traffic Management Systems and Advanced Traffic Information Systems (ATIS) need models accounting for flow changes with time, that is
- Dynamic models able to appropriately describe the time dependencies of traffic demand and the corresponding induced traffic flows
- The Dynamic Traffic Assignment Problem (DTA) is the extension of the Traffic Assignment Problem able of determining such time varying link or path flows.
- DTA should have the capability of describing how traffic flow patterns evolve in time and space on the network (Mahmassani 2001).

DUE FORMULATION

- It can be shown that the DUE approach can be implemented in terms of solving the following mathematical model:

$$[\tau_{rsp}(t) - \theta_{rs}(t)] f_{rsp}(t) = 0 \quad \forall p \in P_{rs}(t), \forall (r, s) \in \mathfrak{I}, t \in [0, T]$$

$$\tau_{rsp}(t) - \theta_{rs}(t) \geq 0 \quad \forall p \in P_{rs}(t), \forall (r, s) \in \mathfrak{I}, t \in [0, T]$$

$$\tau_{rsp}(t), \theta_{rs}(t), f_{rsp}(t) \geq 0$$

- And the flow balancing equations

$$\sum_{p \in P_{rs}(t)} f_{rsp}(t) = d_{rs}(t) \quad \forall (r, s) \in \mathfrak{I}, t \in [0, T]$$

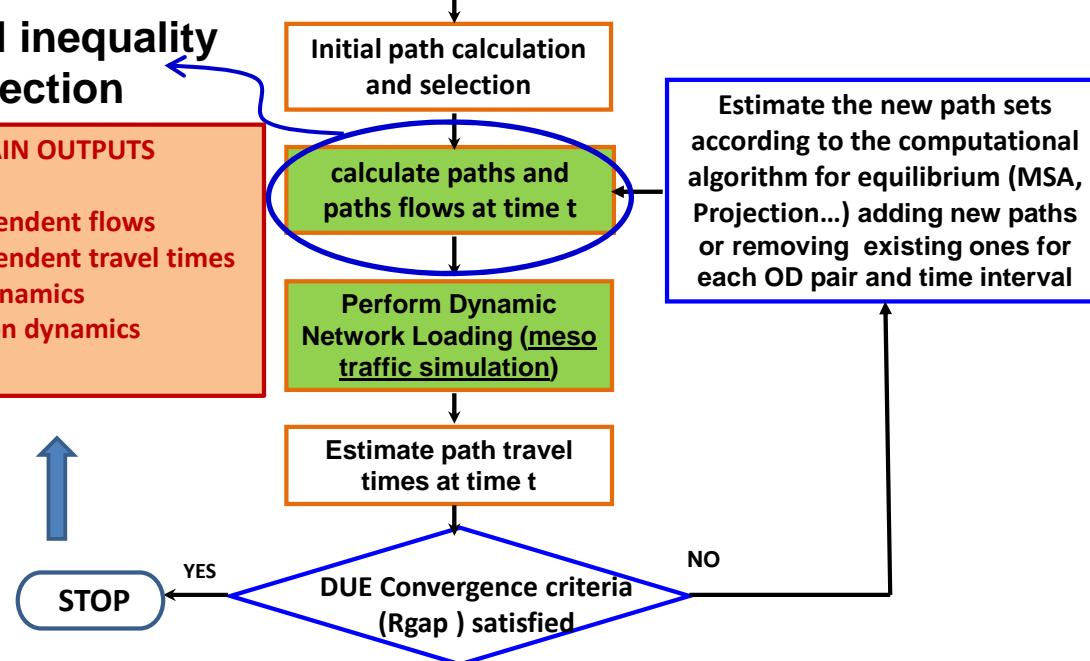
- Where $f_{rsp}(t)$ is the flow on path p from r to s departing origin r at time t
- $\tau_{rsp}(t)$ is the actual path cost from r to s on route p at time t
- $\theta_{rs}(t)$ is the cost of the shortest path from r to s departing from origin r at time t
- $P_{rs}(t)$ is the set of all available paths from r to s at time t
- \mathfrak{I} is the set of all origin-destination pair (r, s) in the network
- $d_{rs}(t)$ is the demand (number of trips) from r to s at time interval t .

Traffic Network Space State Estimation and Short Term Forecasting Based on a Dynamic Traffic Model Mesoscopic Traffic Simulation

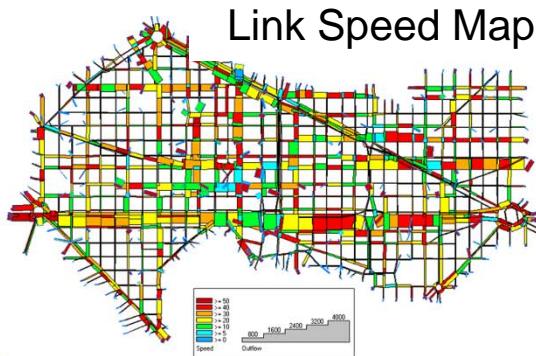
Solve the variational inequality problem (MSA , Projection)

MAIN OUTPUTS

- Time dependent flows
- Time dependent travel times
- Queue dynamics
- Congestion dynamics



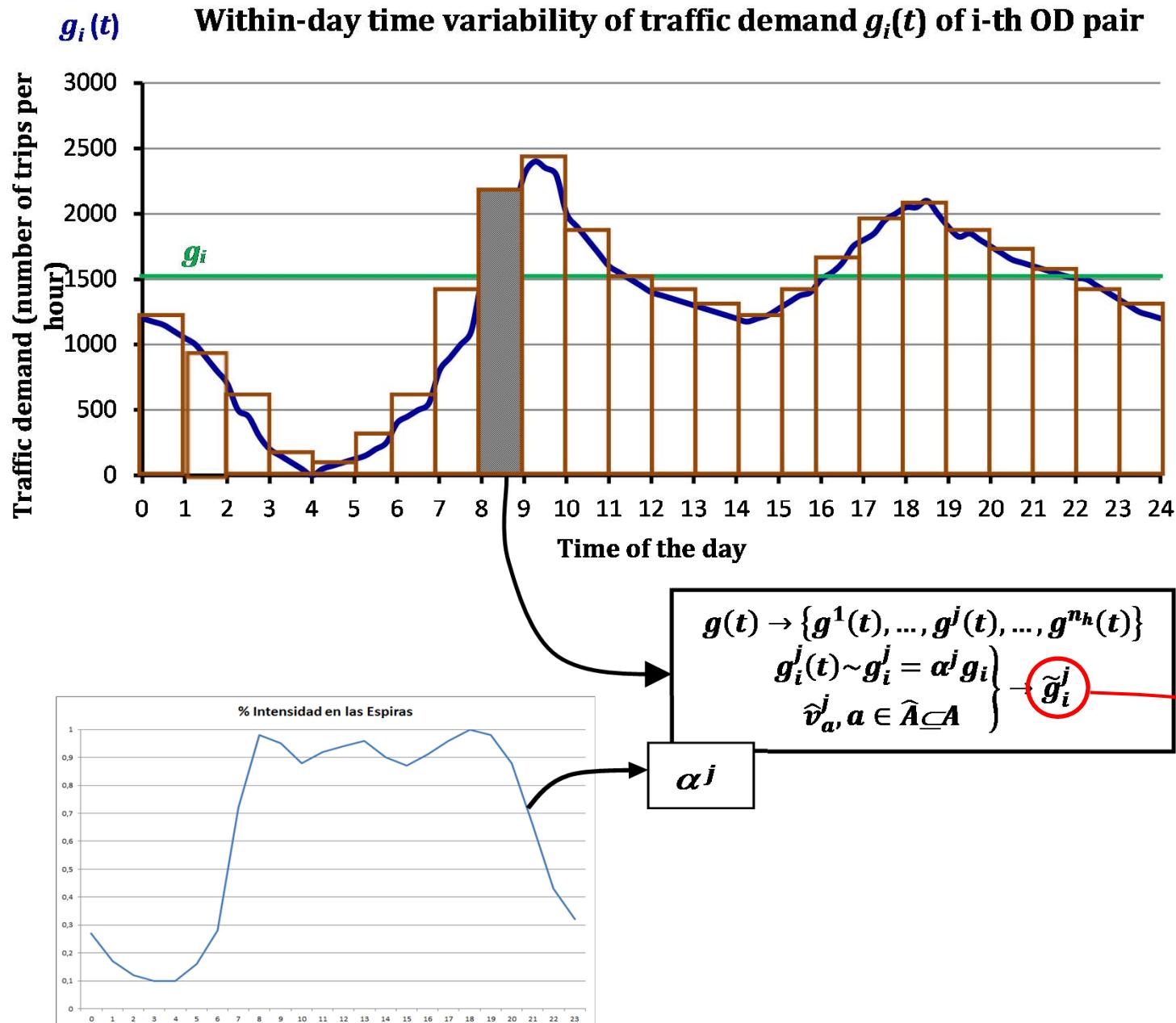
COMPLETE NETWORK INFORMATION



Alternative paths and forecasted path travel times

A map showing alternative paths and forecasted path travel times. The paths are highlighted in different colors (yellow, green, blue) and labeled with their respective travel times. A legend indicates the paths and their travel times.

A COMMON PRACTICAL HEURISTIC APPROACH TO ESTIMATE TIME-SLICED OD MATRICES



THE OD MATRIX IS USUALLY AJUSTED FROM LINK FLOW COUNTS USING A BILEVEL OPTIMIZATION APPROACH

$$\begin{aligned} \min_g F(g, v) &= \gamma_1 F_1(g, \hat{g}) + \gamma_2 F_2(v, \hat{v}) \\ \text{s.t.: } v &= \text{assign}(g) \\ v, g &\geq 0 \end{aligned}$$

Upper level
 γ_1, γ_2 weights, F_1, F_2 Distance Functions
 Non Linear Optimization Problem

$$\underset{g, v}{\text{MIN}} F(g, v) = \gamma_1 F_1(g, \hat{g}) + \gamma_2 F_2(v(g), \hat{v})$$

$$g \in \Omega$$

Lower level
 User Equilibrium Traffic Assignment

$$v(g) = \arg \min \sum_{a \in A} \int_0^{v_a} s_a(x) dx$$

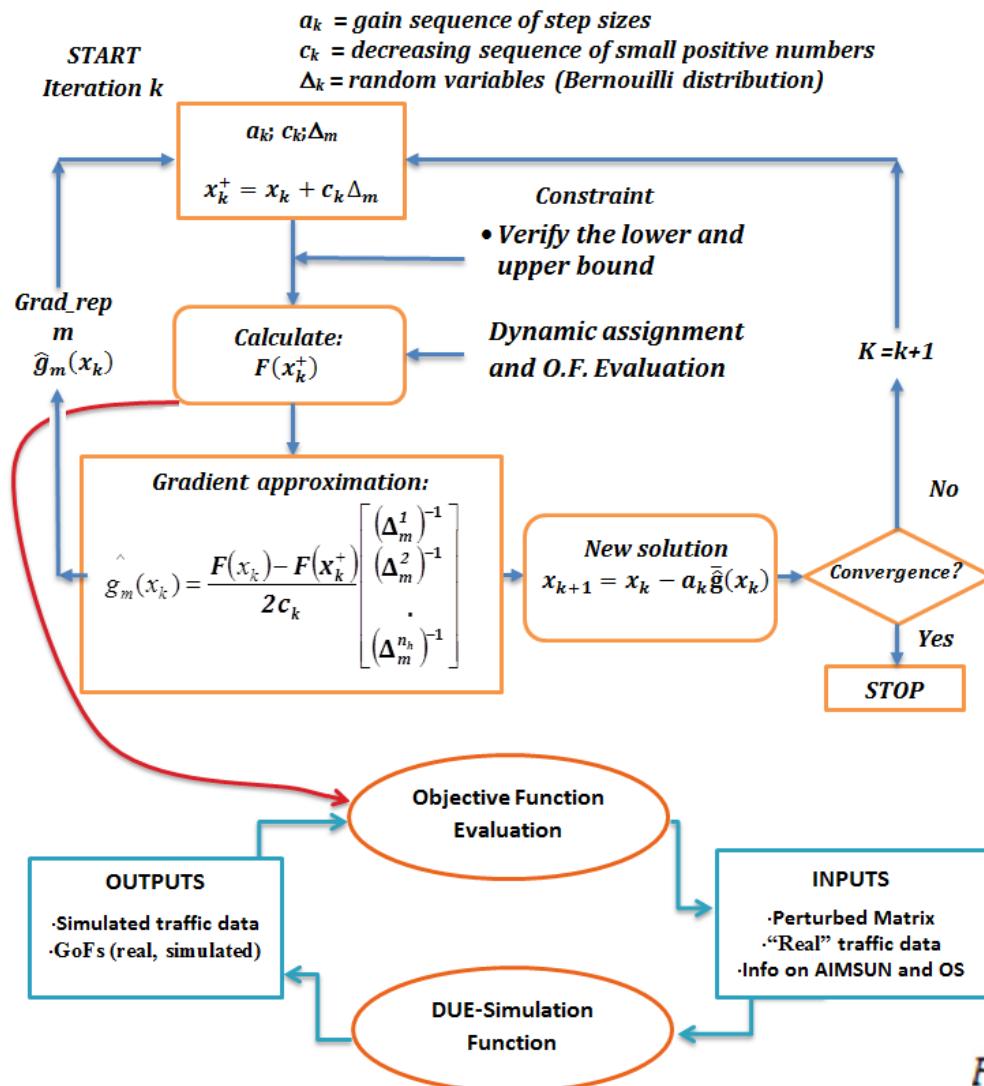
$$\text{s.t. } \sum_{k \in K_i} h_k = g_i, \quad \forall i \in I$$

$$h_k \geq 0, \quad \forall k \in K_i, \quad \forall i \in I$$

$$v_a = \sum_{i \in I} \sum_{k \in K_i} \delta_{ak} h_k$$

A MODIFIED BILEVEL IN WHICH THE LOWER LEVEL EQUILIBRIUM ASSIGNMENT IS REPLACED BY A DUE IMPROVED ACCOUNTING FOR ICT (BLUETOOTH) MEASURED TRAVEL TIMES

A BILEVEL –DUE (*)



- Replace the lower level assignment problem by a DUE
- Conducted with Aimsun Meso in the computational experiences in EU COST ACTION, TU903, MULTITUDE
- Solve upper level optimization

$$\begin{aligned} \text{MIN } F(g^1 \dots g^{nh}) &= \sum_i^n \gamma_i F_i(x^1 \dots x^{nh}; \hat{x}^1 \dots \hat{x}^{nh}) \\ (g^{lw1} \dots g^{lwn_h}) &\leq (g^1 \dots g^{nh}) \leq (g^{ub1} \dots g^{ubnh}) \\ \sum_{i=1}^{nh} G_o^i &\leq G_o^*, \forall o \in \{\text{Origins Set}\} \end{aligned}$$

- by a derivative free method based on Simultaneous Perturbation Stochastic Approximation (SPSA) that evaluates the objective function

$$F_i(x^1 \dots x^{nh}; \hat{x}^1 \dots \hat{x}^{nh}) = (\mathbf{x} - \hat{\mathbf{x}})^T V_i^{-1} (\mathbf{x} - \hat{\mathbf{x}}), i = 1, 2, 3$$

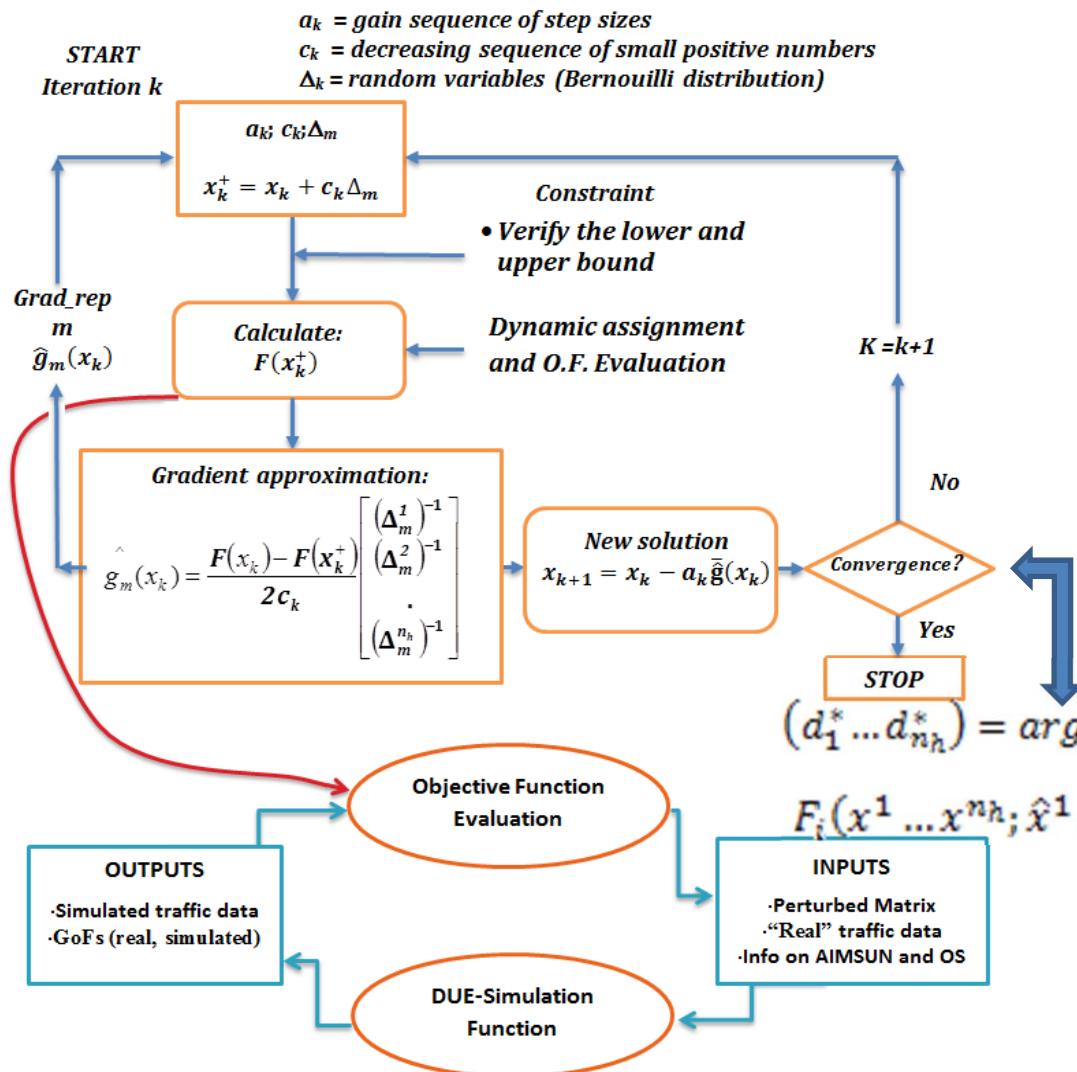
(*) Cipriani E., Florian M., Mahut M. and Nigro M. (2011), A gradient approximation approach for adjusting temporal origin-destination matrices, *Transportation Research Part C* 19 270–282

• by simulation

A MODIFIED SPSA ALGORITHM USING PROJECTED GRADIENT AND TRUST REGION

J. Barceló, L. Montero A robust framework for the estimation of dynamic OD trip matrices for reliable traffic management. 18th Euro Working Group on Transportation, EWGT 2015, 14-16 July 2015, Transportation Research Procedia 10 (2015) 134 – 144

ENHANCED BILEVEL-DUE APPROACH INCLUDING BLUETOOTH MEASURED TRAVEL TIMES



- The objective function has now 4 terms, for distances:
- Between measured and estimated OD terms, link flows, link speeds and
- Travel times between pairs of Bluetooth antennas along specific subpaths

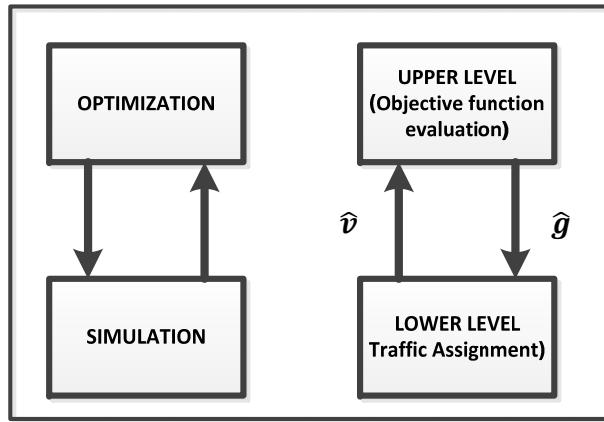
$$f_4(t_1 \dots t_{n_h}, \hat{t}_1 \dots \hat{t}_{n_h})$$

$$\min_{(x_1 \dots x_{n_h}) \geq 0} \left[\sum_{i=1}^m \gamma_i f_i(x^1 \dots x^{n_h}; \hat{x}^1 \dots \hat{x}^{n_h}) \right]$$

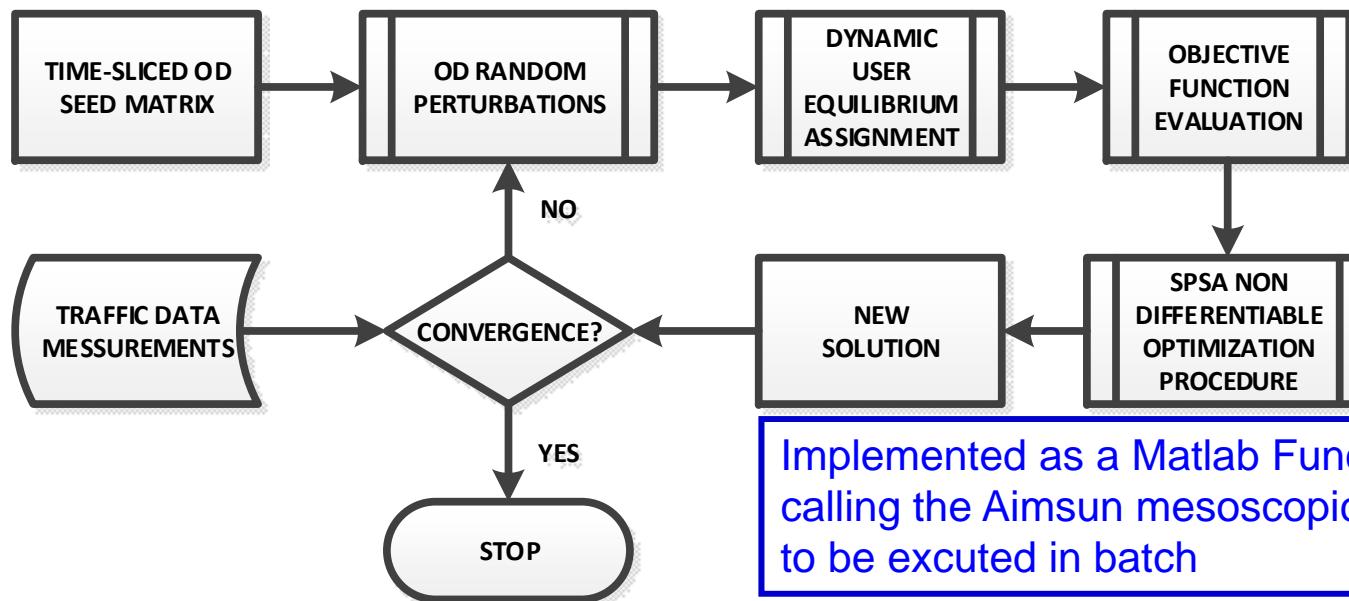
$$F_i(x^1 \dots x^{n_h}; \hat{x}^1 \dots \hat{x}^{n_h}) = (\mathbf{x} - \hat{\mathbf{x}})^T V_i^{-1} (\mathbf{x} - \hat{\mathbf{x}}), i = 1, 2, 3, 4$$

- SPSA has been modified to accomodate the new terms
- Estimated travel times have to be computed from Mesoscopic model

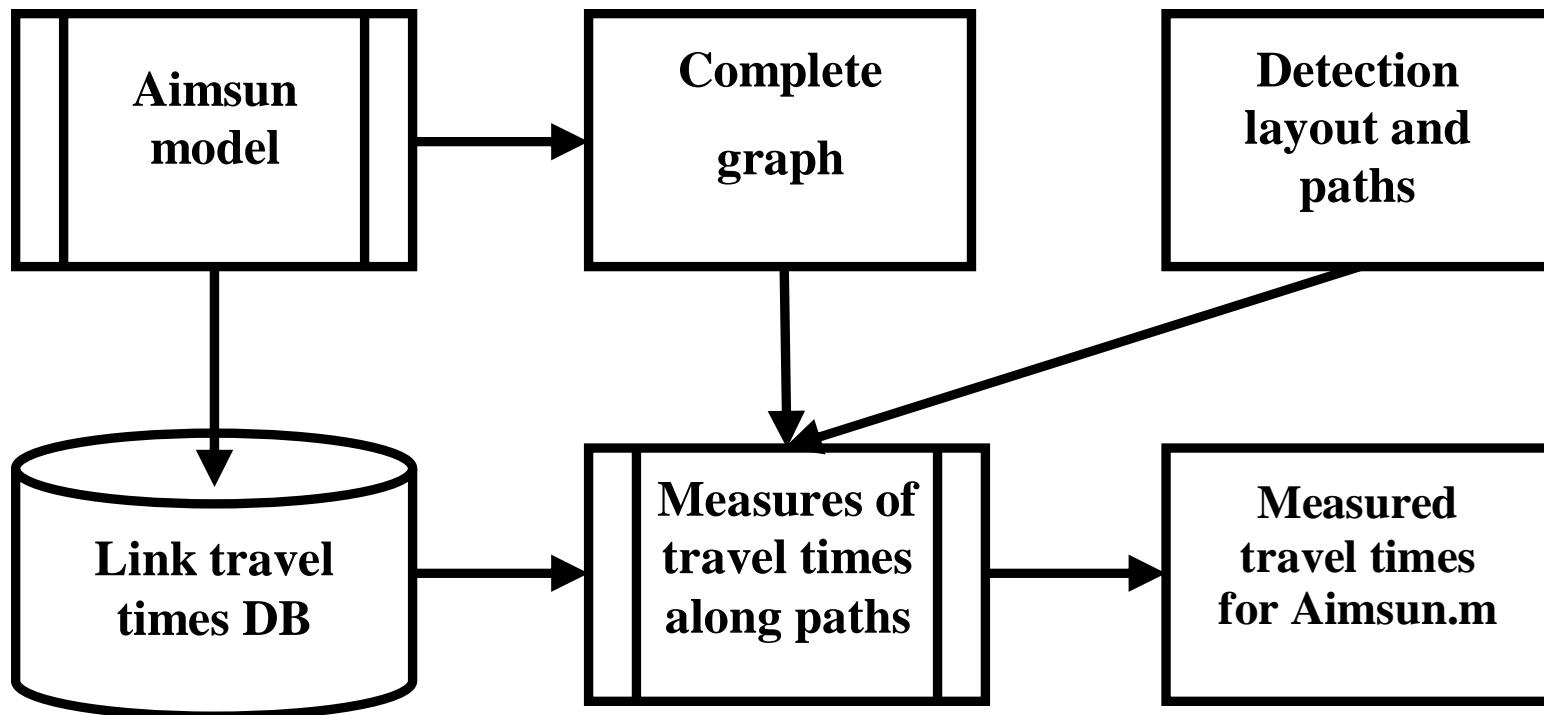
OUTLINE OF THE SPSA BILEVEL DUE ASSIGNMENT



Iteration k
 $\text{Matrix } g^k \rightarrow \text{Call to DUE-Simulation Function} \rightarrow \text{objective}$
 M gradient approximations
 $g^k \rightarrow \text{Perturbation } (g^{k+})$
 $\text{Matrix } g^{k+} \rightarrow \text{Call to DUE-Simulation} \rightarrow \text{objectiveplus}$
 $\text{Gradient} = ((\text{objectiveplus} - \text{objective})/c_k)^* (\text{SPV});$



INTERMEDIATE STEP TO ESTIMATE PATH TRAVEL TIMES BETWEEN PAIRS OF BLUETOOTH ANTENNAS



MODIFIED SPSA

- Replace gradient optimization by conjugated gradient optimization:

$$x_{k+1} = x_k - \alpha_k (\bar{g}(x_k) + \beta \bar{g}(x_{k-1})) \quad \beta = \frac{\|\bar{g}(x_k)\|^2}{\|\bar{g}(x_{k-1})\|^2}$$

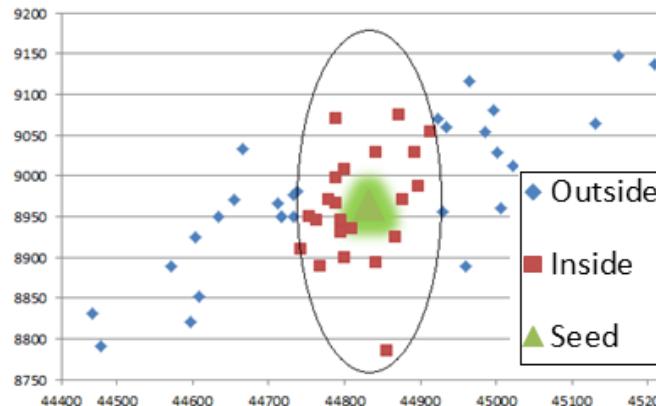
- Restrict the search to a trust region to build, at each iteration, a search range which “trusts” in a neighborhood of the current solution.
 - Analyze the size and number of trips of the seed matrix.
 - Based on this analysis, a search range is established for each time slice in particular and for the number of trips of the entire matrix in general.
 - Let n_s be the number of time slices. Then the trust region is:

$$(1 - \gamma_1) * TS_j(\hat{d}) < TS_j(X^+) < (1 + \gamma_1) * TS_j(\hat{d}) \quad \gamma_1 \in (0.01, 0.1)$$

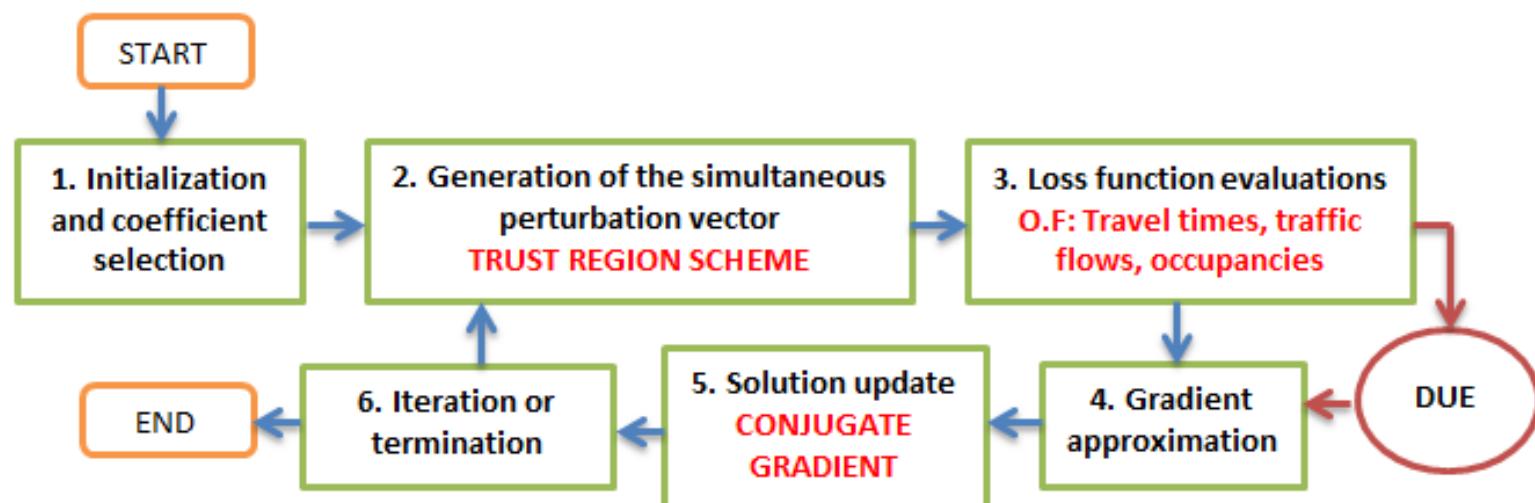
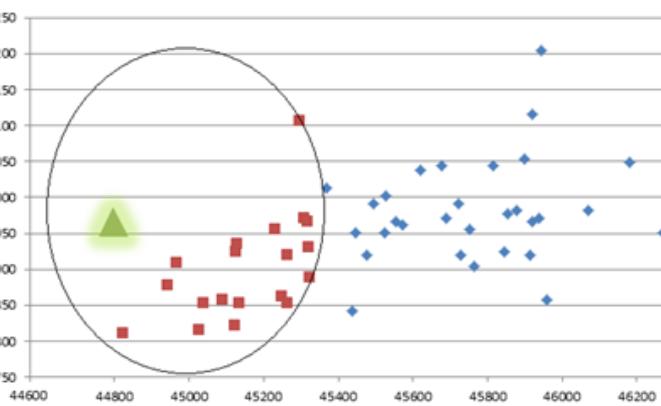
$$(1 - \gamma_2) * \hat{d} < X^+ < (1 + \gamma_2) * \hat{d} \quad \gamma_2 \leq \gamma_1$$

BILEVEL DUE MODIFIED SPSA ALGORITHM (CONJUGATED GRADIENT & TRUST REGION)

a) Trust Region

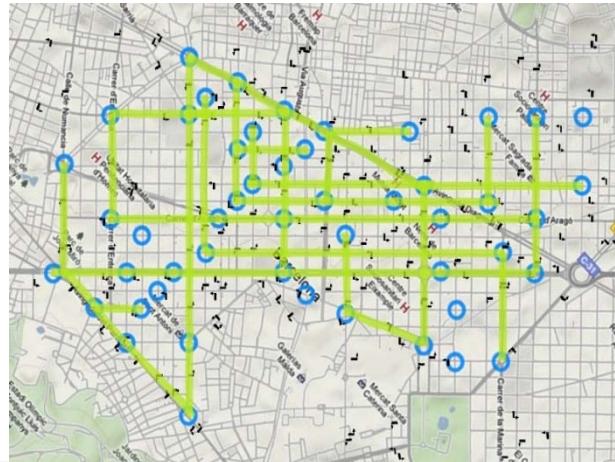


b) Trust Region to update an old matrix



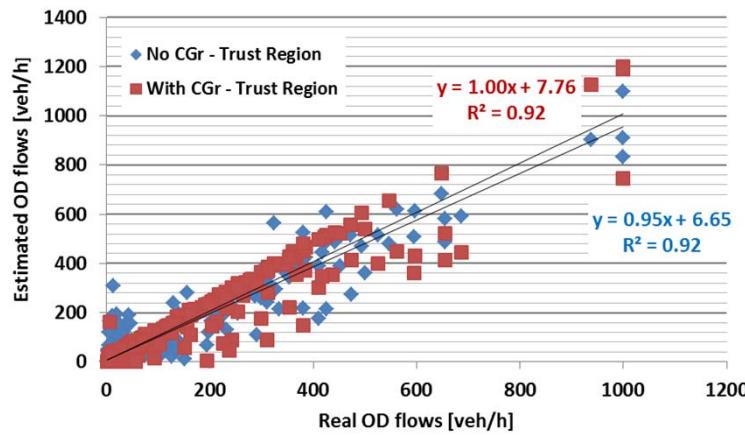
COMPUTATIONAL RESULTS (BARCELONA & VITORIA)

Barcelona's Central Business District (CBD), Eixample, 2111 sections, 1227 nodes 120 generation centroids, 130 destination centroids (877 non-zero OD pairs) 116 Loop detector Stations & 50 Bluetooth Antennas



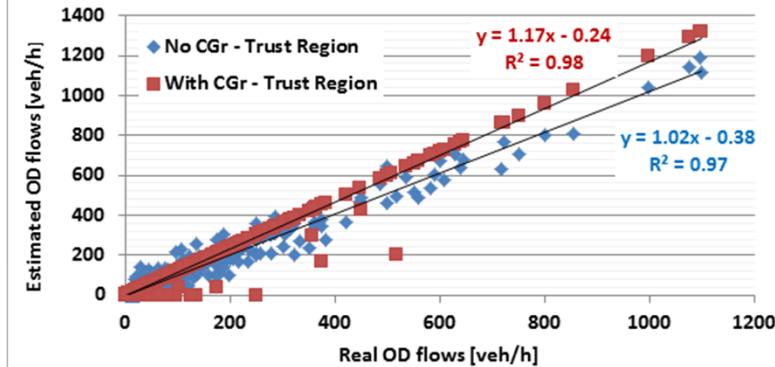
NME (Normalized Mean Error) - EIXAMPLE

OD Flow Comparison - EIXAMPLE



NME (Normalized Mean Error) - VITORIA

OD Flow Comparison - VITORIA

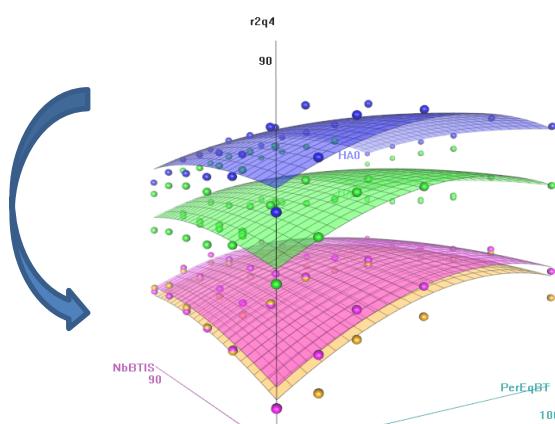


Vitoria (Basc 57 centroids and 2800 intersections. 389 loop detectors and 50 ICT sensors

FROM OFF-LINE TO ON LINE OD ESTIMATION



Identification of time-dependent mobility patterns in terms of Origin-Destination (OD) Matrices Exploiting ICT measurements



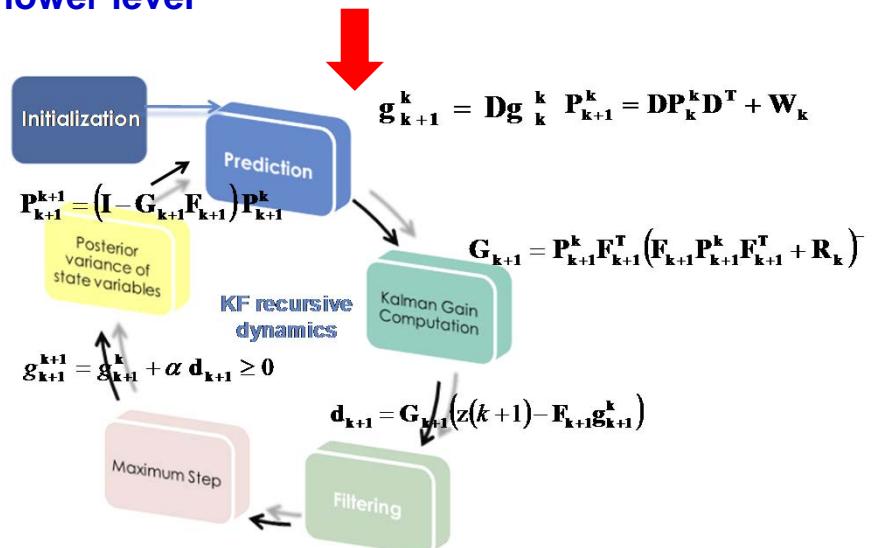
- Factors determining the quality of the estimation:**
1. % technology penetration
 2. Detection layout
 3. Input OD seed

Off-line estimation of a good input OD seed per time interval

$$\begin{aligned} \min_g F(g, v) &= \gamma_1 \cdot F_1(g, \hat{g}) + \gamma_2 \cdot F_2(v, \tilde{v}) \\ \text{s.t.: } v &= \text{assign}(g) \\ v, g &\geq 0 \end{aligned}$$

Nonlinear bilevel nondifferentiable optimization problem solved using:

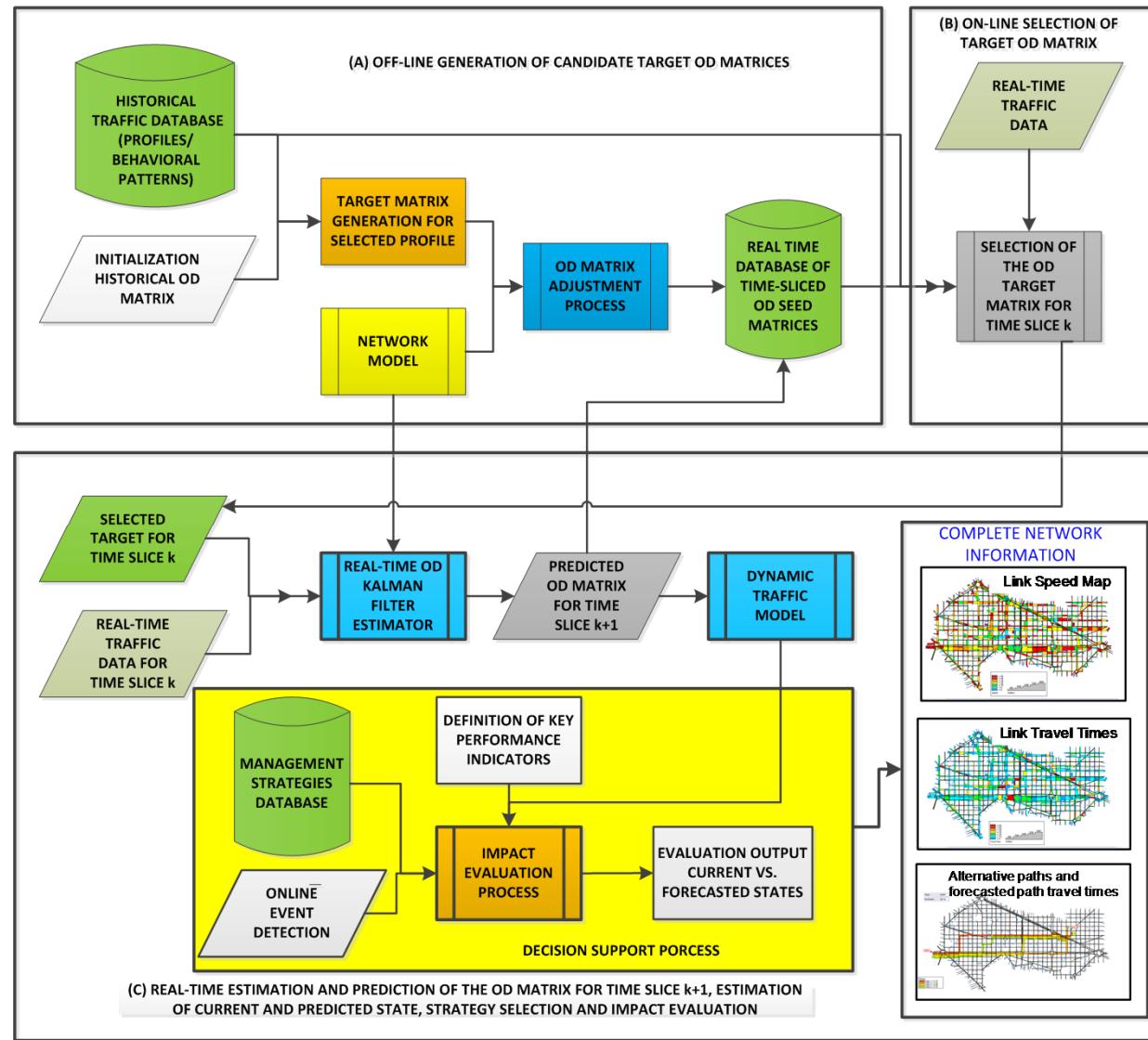
- A special version of Stochastic Perturbation Stochastic Approximation at the upper level
- A Dynamic User Equilibrium Assignment at the lower level



Online Ad Hoc Kalman Filter to estimate the time dependent OD

Barceló, J., Gilliéron, F., Linares, M.P., Serch, O., Montero, L., (2012). Exploring Link Covering and Node Covering Formulations of Detection Layout Problem. *Transportation Research Records* 2308, pp.17-26.
 Barceló, J., Montero, L., Bullejos, M., Linares, M.P., Serch, O., (2013). Robustness and computational efficiency of a Kalman Filter estimator of time dependent OD matrices exploiting ICT traffic measurements. *TRR Transportation Research Records: Journal of the Transportation Research Board*, No.2344. pp.31-39.

CONCEPTUAL ARCHITECTURE OF THE DECISION SUPPORT SYSTEM FOR ADVANCED TRAFFIC MANAGEMENT AND INFORMATION



CONCLUSIONS

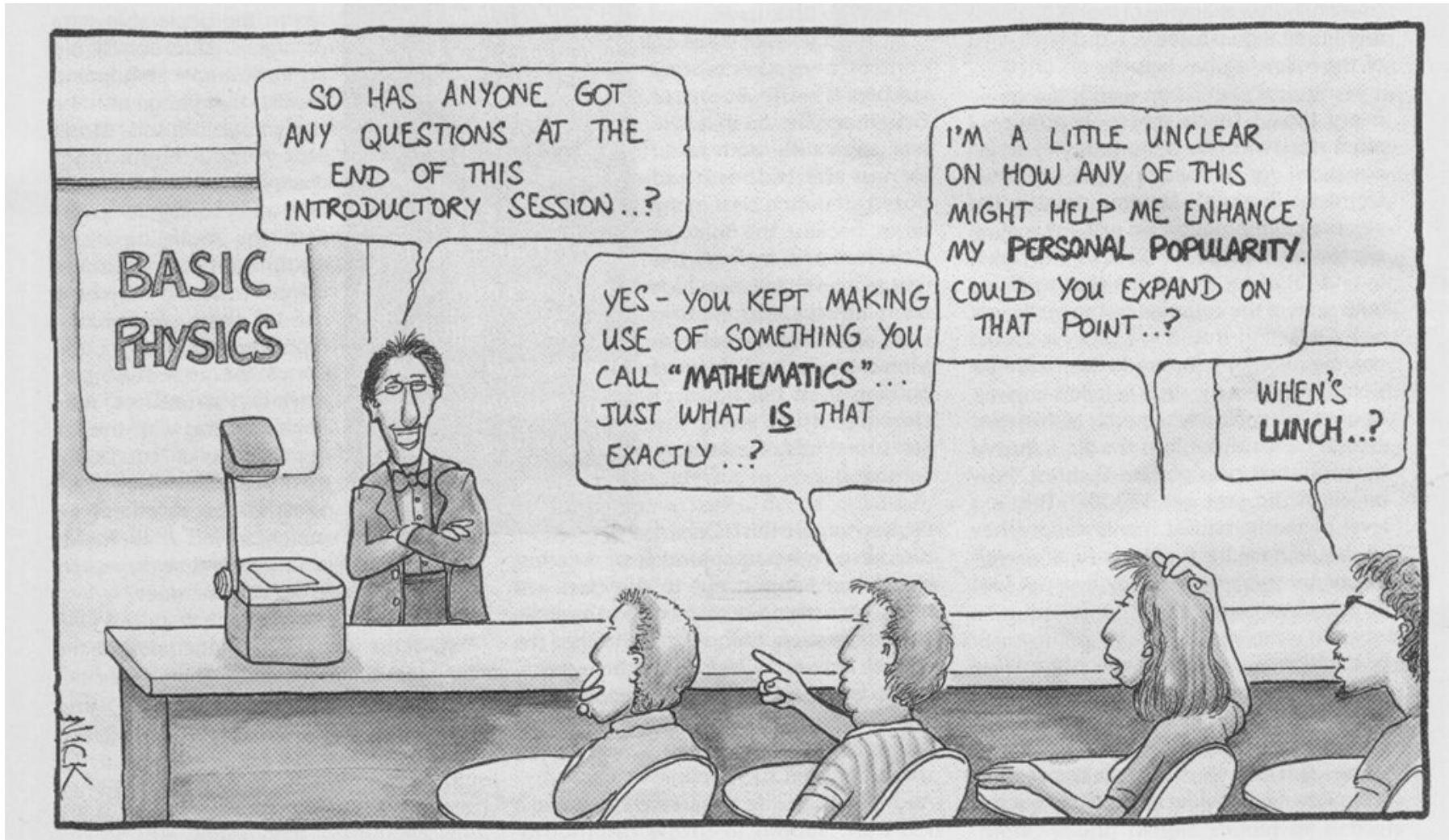
- ICT measures can be exploited by the modified bilevel, which heuristically solves the lower level optimization with a DUE using a mesoscopic simulation for the DNL.
- However, the computational times make the measures useful only for off-line applications.
- It also provides a quite good time-sliced OD that is suitable for the initialization of Kalman Filter for real-time applications when we require the detection layout, the level of ICT penetration and initialization quality.

REFERENCES

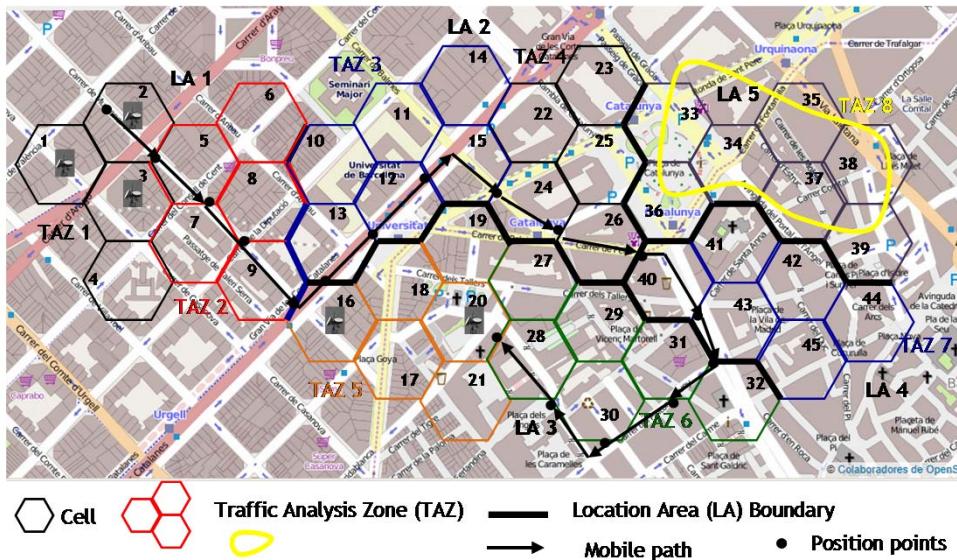


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THANK YOU VERY MUCH FOR YOUR ATTENTION



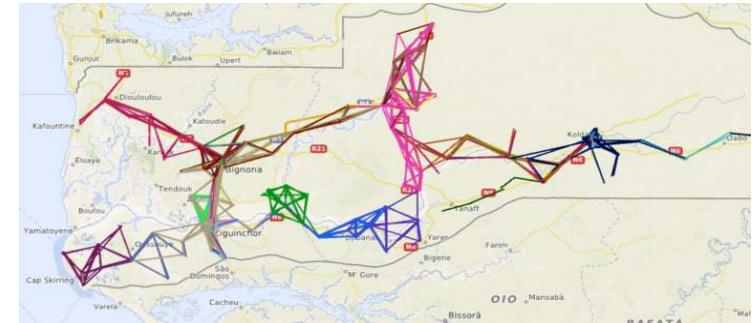
EXPLOITING MOBILE PHONE DATA (*tracking cell phones*)



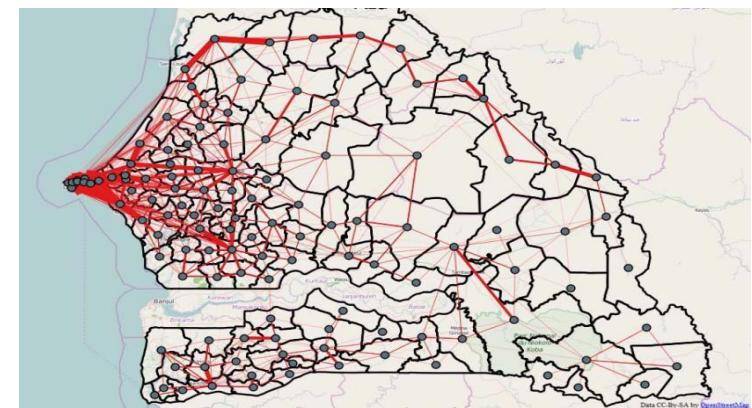
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Example of sequence aggregates



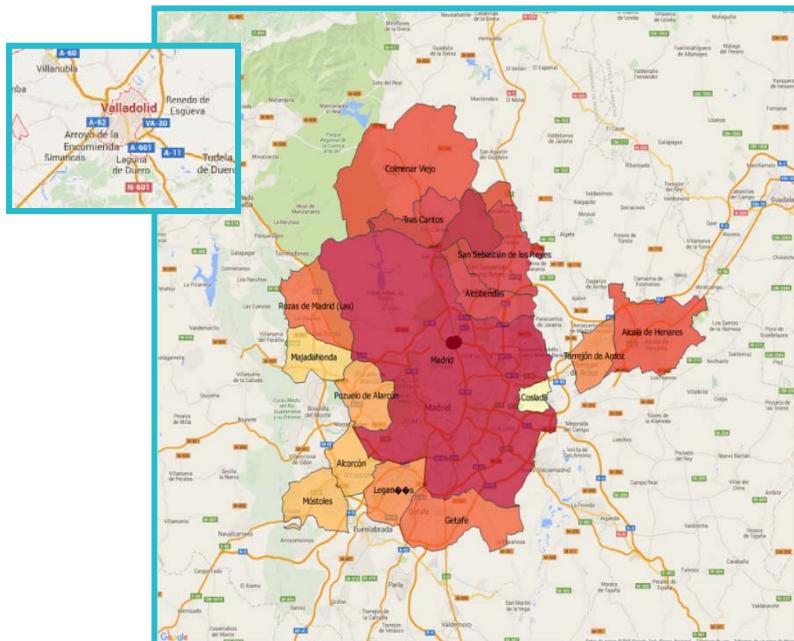
OD demand on the census tract level

MOBILITY KNOWLEDGE ACQUISITION ⇒ DATA COLLECTION (mobile devices) ⇒ BIG DATA DYNAMIC INSIGHTS Smart Steps

<https://dynamicinsights.Telefonica.com/blog/488/smart-steps-2>



WHICH MUNICIPALITIES
GENERATE MOST TRAFFIC IN THE
NUDO DE MANOTERAS?



**EXTRACTION**

Mobile event data extracted and stored from our network.

**ANONYMIZATION**

Personal data eliminated and hashed with an ID.

**EXTRAPOLATION**

Algorithms applied to represent entire population of Spain.

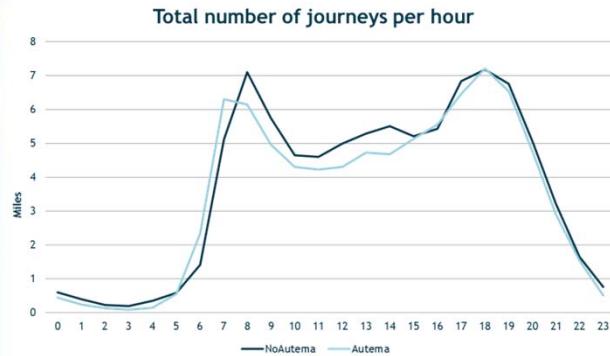
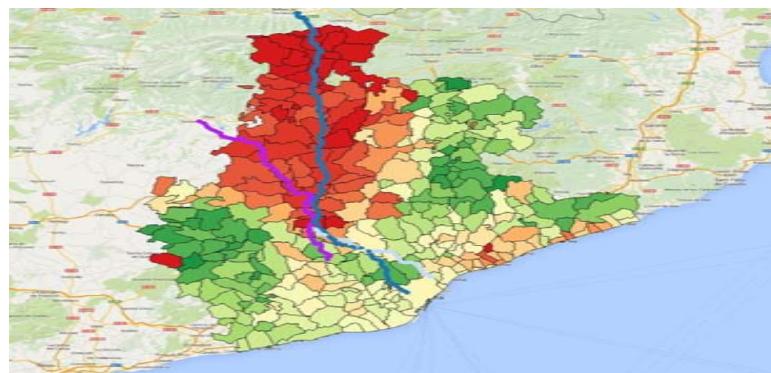
**AGGREGATION**

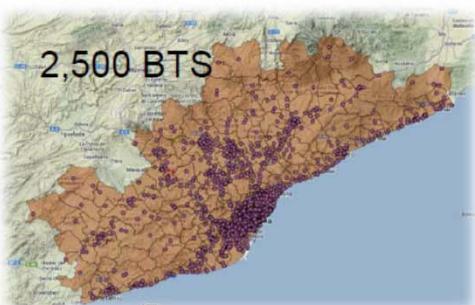
IDs grouped to crowd data, no individual is identifiable.



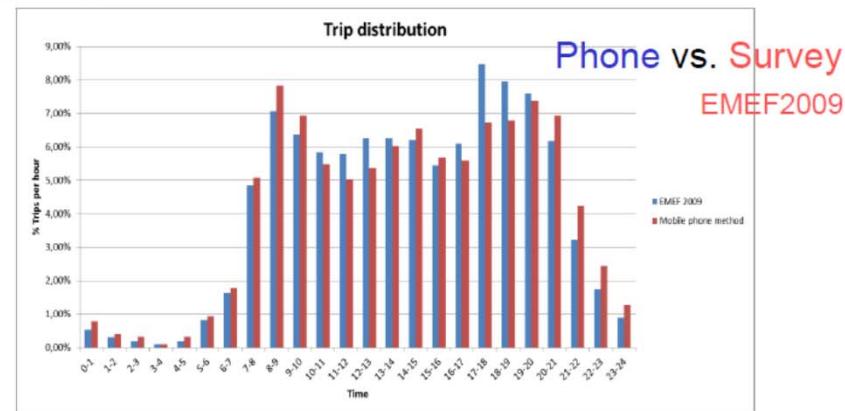
Smart Steps

Analysis of the traffic on the Manresa - San Cugat del Valles road. OD Matrix for all surrounding areas of the road.



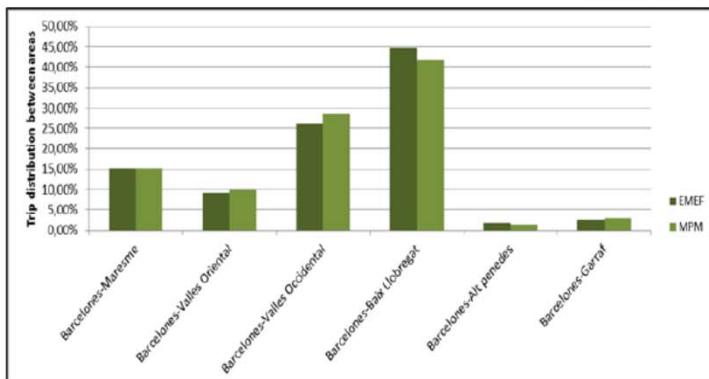


ODs from mobile phone data



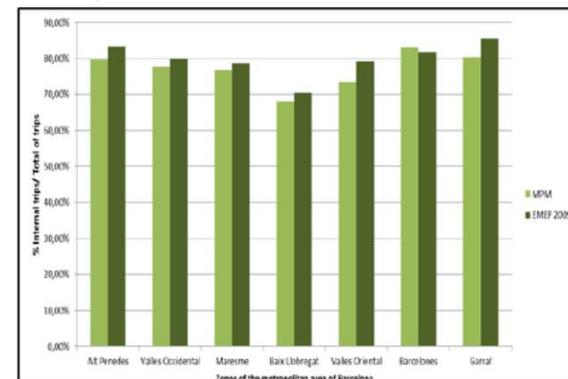
LOW COST ODs

Trip distribution (Barcelonès)

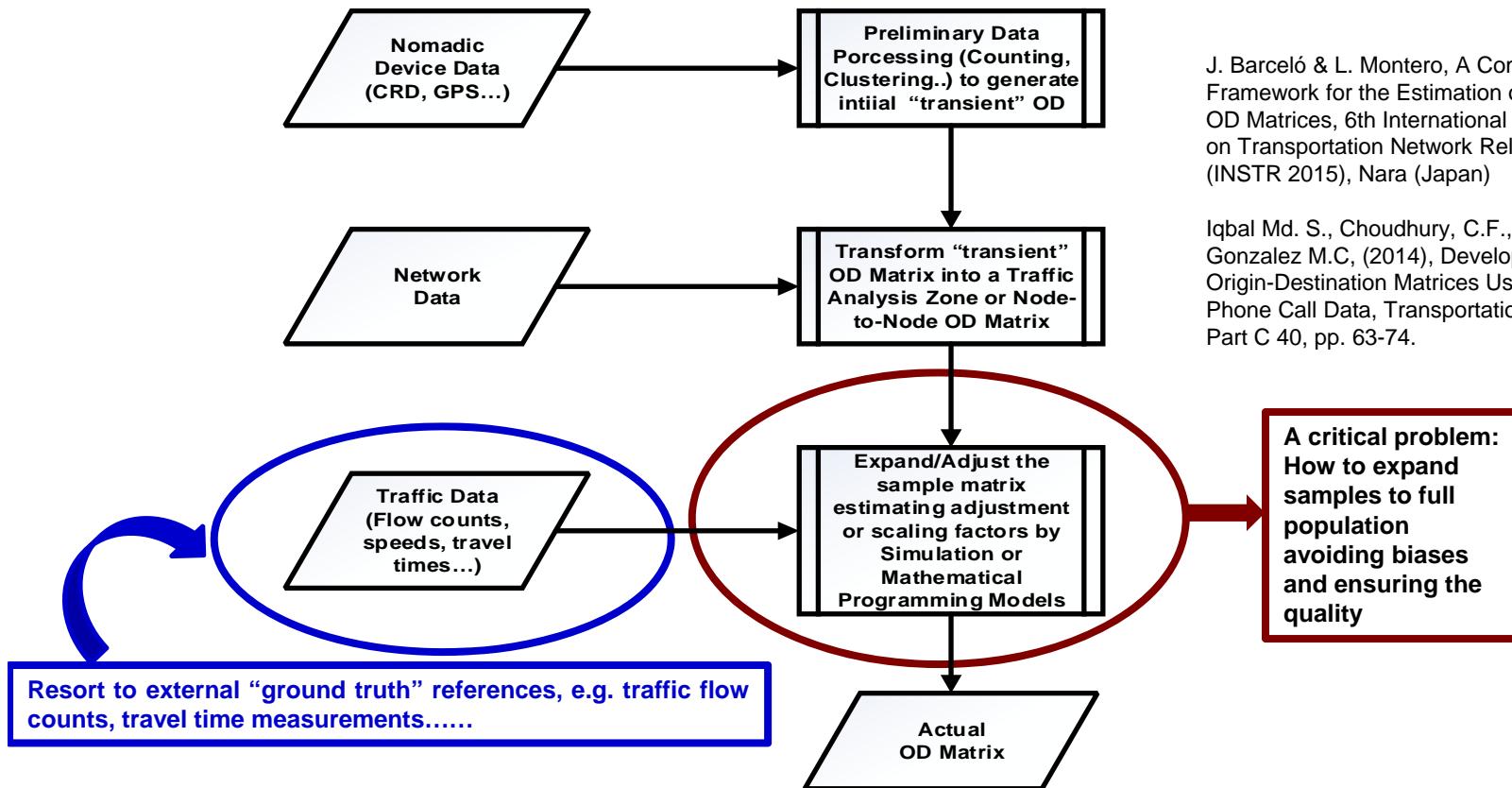


Phone vs. Survey

Intra-zone trips (Municipalities)



CONCEPTUAL FRAMEWORK FOR THE ESTIMATION OF OD MATRICES COMBINING NOMADIC DEVICES DATA AND TRAFFIC DATA



J. Barceló & L. Montero, A Computational Framework for the Estimation of Dynamic OD Matrices, 6th International Symposium on Transportation Network Reliability (INSTRE 2015), Nara (Japan)

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